

Quiz 7  
Econ 526 - Introduction to Econometrics

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Name:

[Same dataset from Quiz 4 & 5] Consider a random sample with the Grade Point Average (GPA) and standardized test scores (ACT), along with the performance in an introductory economics course, for students at a large public university. The variable to be explained is *score*, which is the final score in the course measured as a percentage. The econometric model is:

$$\log(\text{score}) = \beta_0 + \beta_1 \text{hsgpa} + \beta_2 \log(\text{actmth}) + \beta_3 \text{colgpa} + u$$

where *hsgpa* is the high school GPA,  $\log(\text{actmth})$  is the natural logarithm of the ACT in math and *colgpa* is the college GPA of the student prior to take the economics course.

The *R* output is:

**Regression (A)**

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                        Dependent variable:
                        -----
                        log(score)
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hsgpa                    0.0274
                        (0.0204)

log(actmth)              0.3082
                        (0.0388)

colgpa                   0.1784
                        (0.0125)

Constant                 2.7073
                        (0.1119)

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Observations              814
R2                        0.3704
Adjusted R2               0.3681
Residual Std. Error      0.1662 (df = 810)
F Statistic              158.8443 (df = 3; 810)
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Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	2.70730	0.11192	?	< 2e-16
hsgpa	0.02741	0.02037	?	?
log(actmth)	0.30816	0.03881	?	6.7e-15
colgpa	0.17840	0.01250	?	< 2e-16

SECTION A - MULTIPLE CHOICE

12%

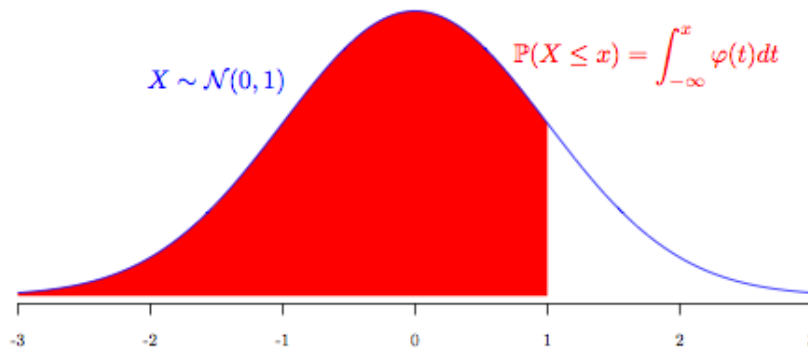
1. Consider the **Regression (A)**. Suppose you want to test whether  $\beta_1 > 0$  (one-sided). What is  $t_{\hat{\beta}_1}$  equal to?
  - A. 0.7445
  - B. 24.1939
  - C. 1.3431
  - D. 0.0413

- 12% 2. Consider the **Regression (A)** again. Suppose you want to test whether  $\beta_1 = 0$  (two-sided). Evaluate the statements below and determine which one is correct.
- We can reject  $H_0$  at 5% significance level, but not at 1% significance level.
  - We can reject  $H_0$  at 10% significance level, but not at 5% significance level.
  - We can reject  $H_0$  at 1% significance level, but not at 0.1% significance level.
  - We cannot reject  $H_0$  at any significance level less than or equal to 10%.
- 12% 3. Consider the **Regression (A)** again. Suppose you want to test whether  $\beta_3$  is statistically significant. Evaluate the statements below and determine which one is correct.
- $\hat{\beta}_3$  is statistically significant at 1% significance level.
  - $\hat{\beta}_3$  is NOT statistically significant at 1% significance level.
  - $\hat{\beta}_3$  is NOT statistically significant at 5% significance level.
  - $\hat{\beta}_3$  is NOT statistically significant at 10% significance level.
- 12% 4. Consider the **Regression (A)** again. Suppose you want to test whether  $\beta_2$  is statistically significant. Evaluate the statements below and determine which one is correct.
- $\hat{\beta}_2$  is statistically significant at 0.1% significance level.
  - $\hat{\beta}_2$  is statistically significant at 1% significance level.
  - $\hat{\beta}_2$  is statistically significant at 5% significance level.
  - All the above.
- 12% 5. Consider the **Regression (A)** again. Suppose you want to test whether the elasticity of *score* with respect *actmth* is unitary, i.e., equal to 1 or not. Evaluate the statements below and determine which one is correct.
- We can NOT reject the null hypothesis at 2% significance level.
  - the  $t$  statistic provides **no (or little)** evidence against the null hypothesis at small significance levels ( $< 1\%$ ).
  - the  $t$  statistic provides evidence against the null hypothesis at small significance levels ( $< 1\%$ ).
  - $\hat{\beta}_2$  is NOT statistically different from 1 at 5% significance level.
- 12% 6. Assume that the **Classical Linear Model (CLM)** assumptions hold. As can be seen in the regression output,  $\hat{\beta}_3 = 0.178$  and  $se(\hat{\beta}_3) = 0.0125$ . What is the distribution of  $\frac{0.178 - \beta_3}{0.0125}$ ?
- $t_{df}$ , where  $df = 3$
  - $F_{(3,810)}$
  - $N(0, 0.0125^2)$
  - $t_{df}$ , where  $df = 810$

## SECTION B - TRUE OR FALSE

- 10% 1. The 95% confidence interval for  $\beta_1$  is approximately  $[-0.013, 0.067]$ .  
 True    False
- 9% 2. Consider any multiple linear regression. Knowing that you can reject  $H_0$  for a specific parameter at 1% significance level, then you should be able to reject the  $H_0$  at 2% significance level.  
 True    False
- 9% 3. Consider any multiple linear regression. Knowing that you can reject  $H_0$  for a specific parameter at 1% significance level, then you should be able to reject the  $H_0$  at 0.1% significance level.  
 True    False

Standard Normal Distribution



	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990

$t$ -distribution

TABLE G.2 Critical Values of the $t$ Distribution						
		Significance Level				
1-Tailed:		.10	.05	.025	.01	.005
2-Tailed:		.20	.10	.05	.02	.01
	1	3.078	6.314	12.706	31.821	63.657
	2	1.886	2.920	4.303	6.965	9.925
	3	1.638	2.353	3.182	4.541	5.841
	4	1.533	2.132	2.776	3.747	4.604
	5	1.476	2.015	2.571	3.365	4.032
	6	1.440	1.943	2.447	3.143	3.707
	7	1.415	1.895	2.365	2.998	3.499
	8	1.397	1.860	2.306	2.896	3.355
	9	1.383	1.833	2.262	2.821	3.250
	10	1.372	1.812	2.228	2.764	3.169
D e g r e e s  o f  F r e e d o m	11	1.363	1.796	2.201	2.718	3.106
	12	1.356	1.782	2.179	2.681	3.055
	13	1.350	1.771	2.160	2.650	3.012
	14	1.345	1.761	2.145	2.624	2.977
	15	1.341	1.753	2.131	2.602	2.947
	16	1.337	1.746	2.120	2.583	2.921
	17	1.333	1.740	2.110	2.567	2.898
	18	1.330	1.734	2.101	2.552	2.878
	19	1.328	1.729	2.093	2.539	2.861
	20	1.325	1.725	2.086	2.528	2.845
21	1.323	1.721	2.080	2.518	2.831	
22	1.321	1.717	2.074	2.508	2.819	
23	1.319	1.714	2.069	2.500	2.807	
24	1.318	1.711	2.064	2.492	2.797	
25	1.316	1.708	2.060	2.485	2.787	
26	1.315	1.706	2.056	2.479	2.779	
27	1.314	1.703	2.052	2.473	2.771	
28	1.313	1.701	2.048	2.467	2.763	
29	1.311	1.699	2.045	2.462	2.756	
30	1.310	1.697	2.042	2.457	2.750	
40	1.303	1.684	2.021	2.423	2.704	
60	1.296	1.671	2.000	2.390	2.660	
90	1.291	1.662	1.987	2.368	2.632	
120	1.289	1.658	1.980	2.358	2.617	
$\infty$	1.282	1.645	1.960	2.326	2.576	

Source: Wooldridge, Jeffrey M. *Introductory Econometrics*, 2015.